

Name: \_\_\_\_\_

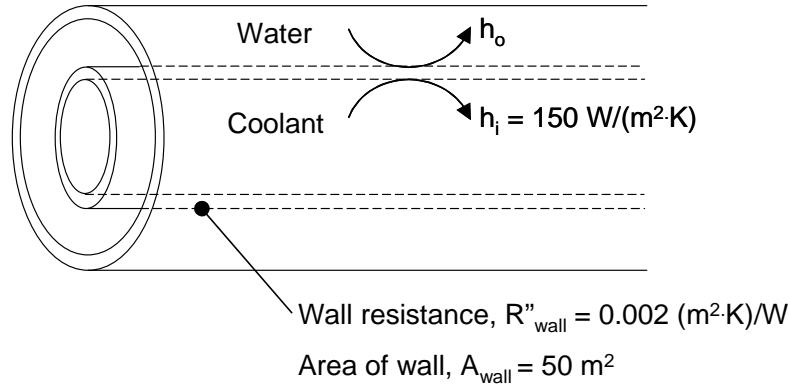
**ME 315: Heat and Mass Transfer**  
**Spring 2008**  
**EXAM 3**  
**Thursday, 17 April 2008**  
**7:00 to 8:00 PM**

**Instructions:** This is an open-book exam. You may refer to your course textbook, your class notes and your graded homework assignments. Show all work clearly for maximum credit.  
**CIRCLE ALL ANSWERS.**

Problem	Score
1	/ 20
2	/ 22
3	/ 18
Total	/ 60

Name: \_\_\_\_\_

1. (20 points) A concentric tube heat exchanger is used to cool water at a mass flow rate of 1 kg/s from 80 °C to 40 °C. The coolant enters at 0 °C and exits at 50 °C. The specific heat for water and coolant are  $c_{p,\text{water}} = 4200 \text{ J/(kg}\cdot\text{K)}$  and  $c_{p,\text{cool}} = 1500 \text{ J/(kg}\cdot\text{K)}$ , respectively. The surface area of the thin-walled tube separating the water and coolant is  $50 \text{ m}^2$ .



- a. (2 points) In order to achieve the desired inlet and outlet temperatures, which concentric tube heat exchanger configuration must be used? Circle the correct configuration below.
- Parallel Flow                      Counter Flow
- b. (4 points) Find the rate of heat transferred from the water to the coolant.
- c. (4 points) What must the mass flow rate of the coolant be in order to remove the desired heat from the water?
- d. (4 points) What is the effectiveness of the heat exchanger?
- e. (6 points) If the heat transfer coefficient on the coolant side is  $h_i = 150 \text{ W/(m}^2\cdot\text{K)}$  and the thin wall between the water and coolant has a resistance of  $R''_{\text{wall}} = 0.002 \text{ (m}^2\cdot\text{K)/W}$ , then what is the heat transfer coefficient on the water side ( $h_o$ )?

Water

$$T_{hi} := (80 + 273)K$$

$$T_{ho} := (40 + 273)K$$

$$c_{ph} := 4200 \frac{J}{kg \cdot K}$$

$$m_{h.dot} := 1 \frac{kg}{s}$$

b )

$$C_h := m_{h.dot} \cdot c_{ph}$$

$$q := C_h \cdot (T_{hi} - T_{ho})$$

c )

$$C_c := \frac{q}{T_{co} - T_{ci}}$$

$$m_{c.dot} := \frac{C_c}{c_{pc}}$$

d )

Therefore,

$$C_{min} := C_c$$

$$q_{max} := C_{min} \cdot (T_{hi} - T_{ci})$$

$$\varepsilon := \frac{q}{q_{max}}$$

Refrigerant

$$T_{ci} := (0 + 273)K$$

$$T_{co} := (50 + 273)K$$

$$c_{pc} := 1500 \frac{J}{kg \cdot K}$$

$$h_i := 150 \frac{W}{m^2 \cdot K}$$

coolant (refrigerant) cooling the water  
water > refig

$$A_{wall} := 50m^2$$

$$R_{wall} := 0.002 \frac{m^2 \cdot K}{W}$$

$$C_h = 4.2 \times 10^3 \frac{W}{K}$$

$$q = 1.68 \times 10^5 W$$

$$C_c = 3.36 \times 10^3 \frac{W}{K}$$

$$m_{c.dot} = 2.24 \frac{kg}{s}$$

$$\varepsilon = 0.625$$

Note that epsilon could also be found using the epsilon - NTU method if they solve for U to get NTU and then use equation 11.29b or Figure 11.11 but this is much more involved since they know q and q\_max.

e )

$$\Delta T_1 := T_{hi} - T_{co}$$

$$\Delta T_2 := T_{ho} - T_{ci}$$

$$\Delta T_{lm} := \frac{\Delta T_1 - \Delta T_2}{\ln\left(\frac{\Delta T_1}{\Delta T_2}\right)}$$

$$\Delta T_{lm} = 34.761 K$$

$$U := \frac{q}{A_{\text{wall}} \cdot \Delta T_{\text{lm}}} \quad U = 96.661 \frac{\text{W}}{\text{m}^2 \cdot \text{K}}$$

$$U_{\text{overall}} := \left( \frac{1}{h_i} + R_{\text{wall}} + \frac{1}{h_o} \right)^{-1}$$

$$h_o := \left( \frac{1}{U} - \frac{1}{h_i} - R_{\text{wall}} \right)^{-1} \quad h_o = 595.682 \frac{\text{W}}{\text{m}^2 \cdot \text{K}}$$

2. (22 points) Consider one side of a flat, mechanically polished, stainless steel surface that is in contact with a fluid and has a square area of  $0.01 \text{ m}^2$  (10 cm on a side). In each of the following two scenarios, **indicate the dominant heat transfer mode(s)** (such as conduction, convection, radiation, etc.) and **determine the input power [W]** required to maintain its surface at 390 K at atmospheric pressure in the following two scenarios:

- a. (11 points) Surface oriented vertically in quiescent air at 300 K.

Air properties at an appropriate temperature:

$$\begin{aligned} \nu_{air} &= 20.9 \times 10^{-6} \left[ \frac{\text{m}^2}{\text{s}} \right] & k_{air} &= 0.03 \left[ \frac{\text{W}}{\text{m} \cdot \text{K}} \right] \\ \mu_{air} &= 208.2 \times 10^{-7} \left[ \frac{\text{kg}}{\text{m} \cdot \text{s}} \right] & \alpha_{air} &= 29.9 \times 10^{-6} \left[ \frac{\text{m}^2}{\text{s}} \right] \\ c_{p,air} &= 1009 \left[ \frac{\text{J}}{\text{kg} \cdot \text{K}} \right] & \text{Pr}_{air} &= 0.7 \\ \rho_{air} &= 0.995 \left[ \frac{\text{kg}}{\text{m}^3} \right] \end{aligned}$$

- b. (11 points) Surface oriented horizontally in quiescent water at 300 K

Saturated water properties (for liquid and vapor) at an appropriate temperature:

$$\begin{aligned} \mu_l &= 279 \times 10^{-6} \left[ \frac{\text{kg}}{\text{m} \cdot \text{s}} \right] & \mu_v &= 12 \times 10^{-6} \left[ \frac{\text{kg}}{\text{m} \cdot \text{s}} \right] & h_{fg} &= 2257 \left[ \frac{\text{kJ}}{\text{kg}} \right] \\ c_{p,l} &= 4217 \left[ \frac{\text{J}}{\text{kg} \cdot \text{K}} \right] & c_{p,v} &= 2029 \left[ \frac{\text{J}}{\text{kg} \cdot \text{K}} \right] & \sigma_{surf,tension} &= 0.059 \left[ \frac{\text{kg}}{\text{s}^2} \right] \\ \rho_l &= 957.8 \left[ \frac{\text{kg}}{\text{m}^3} \right] & \rho_v &= 0.596 \left[ \frac{\text{kg}}{\text{m}^3} \right] \\ k_l &= 0.68 \left[ \frac{\text{W}}{\text{m} \cdot \text{K}} \right] & k_v &= 0.025 \left[ \frac{\text{W}}{\text{m} \cdot \text{K}} \right] \\ \text{Pr}_l &= 1.76 & \text{Pr}_v &= 0.984 \end{aligned}$$

a) Given

$$T_s := 390\text{K}$$

$$T_{\text{inf}} := 300\text{K}$$

$$T_f := \frac{T_s + T_{\text{inf}}}{2}$$

$$T_f = 345\text{K}$$

$$w := 10\text{cm}$$

$$L := 10\text{cm}$$

$$A := w \cdot L$$

$$A = 0.01\text{m}^2$$

$$\sigma := 5.67 \cdot 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4}$$

Air at  $T_f \sim 350\text{K}$

$$\nu_{\text{air}} := 20.9 \cdot 10^{-6} \frac{\text{m}^2}{\text{s}}$$

$$\mu_{\text{air}} := 208.2 \cdot 10^{-7} \frac{\text{kg}}{\text{m} \cdot \text{s}}$$

$$c_{p,\text{air}} := 1009 \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

$$\rho_{\text{air}} := 0.995 \frac{\text{kg}}{\text{m}^3}$$

$$k_{\text{air}} := 0.03 \frac{\text{W}}{\text{m} \cdot \text{K}}$$

$$\alpha_{\text{air}} := 29.9 \cdot 10^{-6} \frac{\text{m}^2}{\text{s}}$$

$$\text{Pr}_{\text{air}} := 0.7$$

for an ideal gas:  $\beta := \frac{1}{T_f}$

$$\text{Ra}_L := \frac{g \cdot \beta \cdot (T_s - T_{\text{inf}}) \cdot L^3}{\nu_{\text{air}} \cdot \alpha_{\text{air}}} \quad \text{Ra}_L = 4.094 \times 10^6 \quad \text{Therefore the flow is laminar.}$$

Any of the following 3 relations could be used to evaluate the  $q_{\text{free convection}}$

Using 9.24

$$C := 0.59 \quad n := \frac{1}{4} \quad \text{Nu}_{\text{Lavg1}} := C \cdot \text{Ra}_L^n \quad \text{Nu}_{\text{Lavg1}} = 26.539 \quad h_1 := \frac{k_{\text{air}} \cdot \text{Nu}_{\text{Lavg1}}}{L}$$

$$h_1 = 7.962 \frac{\text{W}}{\text{m}^2 \cdot \text{K}}$$

Using 9.26

$$\text{Nu}_{\text{Lavg2}} := \left[ 0.825 + \frac{0.387 \cdot \text{Ra}_L^{\frac{1}{6}}}{\left[ 1 + \left( \frac{0.492}{\text{Pr}_{\text{air}}} \right)^{\frac{9}{16}} \right]^{\frac{8}{27}}} \right]^2 \quad \text{Nu}_{\text{Lavg2}} = 24.245 \quad h_2 := \frac{k_{\text{air}} \cdot \text{Nu}_{\text{Lavg2}}}{L}$$

$$h_2 = 7.273 \frac{\text{W}}{\text{m}^2 \cdot \text{K}}$$

Using 9.27

$$\text{Nu}_{\text{Lavg3}} := 0.68 + \frac{0.67 \cdot \text{Ra}_L^{\frac{1}{4}}}{\left[ 1 + \left( \frac{0.492}{\text{Pr}_{\text{air}}} \right)^{\frac{9}{16}} \right]^{\frac{4}{9}}}$$

$$\text{Nu}_{\text{Lavg3}} = 23.775$$

$$h_3 := \frac{k_{\text{air}} \cdot \text{Nu}_{\text{Lavg3}}}{L}$$

$$h_3 = 7.132 \frac{\text{W}}{\text{m}^2 \cdot \text{K}}$$

For stainless steel the emissivity can be found from Table A.11 in the appendix

$$\varepsilon := 0.17$$

Radiation needs to be included since the plate is at a high temperature and can emit to the surroundings. Assume the surrounding temperature is the same as the  $T_{\text{inf}}$ .

$$q_1 := h_1 \cdot A \cdot (T_s - T_{\text{inf}}) + \varepsilon \cdot A \cdot \sigma \cdot (T_s^4 - T_{\text{inf}}^4)$$

$$q_1 = 8.615 \text{ W}$$

$$q_2 := h_2 \cdot A \cdot (T_s - T_{\text{inf}}) + \varepsilon \cdot A \cdot \sigma \cdot (T_s^4 - T_{\text{inf}}^4)$$

$$q_2 = 7.995 \text{ W}$$

$$q_3 := h_3 \cdot A \cdot (T_s - T_{\text{inf}}) + \varepsilon \cdot A \cdot \sigma \cdot (T_s^4 - T_{\text{inf}}^4)$$

$$q_3 = 7.868 \text{ W}$$

$$q_{\text{rad}} := \varepsilon \cdot A \cdot \sigma \cdot (T_s^4 - T_{\text{inf}}^4)$$

$$q_{\text{rad}} = 1.449 \text{ W}$$

b) Water at  $T = 373 \text{ K}$

$$\mu_l := 279 \cdot 10^{-6} \frac{\text{kg}}{\text{m} \cdot \text{s}}$$

$$\mu_v := 12 \cdot 10^{-6} \frac{\text{kg}}{\text{m} \cdot \text{s}}$$

$$h_{\text{fg}} := 2257000 \frac{\text{J}}{\text{kg}}$$

$$c_{p,l} := 4217 \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

$$c_{p,v} := 2029 \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

$$\sigma_{\text{st}} := 0.059 \frac{\text{kg}}{\text{s}^2}$$

$$\rho_l := 957.8 \frac{\text{kg}}{\text{m}^3}$$

$$\rho_v := 0.596 \frac{\text{kg}}{\text{m}^3}$$

$$k_l := 0.68 \frac{\text{W}}{\text{m} \cdot \text{K}}$$

$$k_v := 0.025 \frac{\text{W}}{\text{m} \cdot \text{K}}$$

$$\text{Pr}_l := 1.76$$

$$\text{Pr}_v := 0.984$$

$$T_{\text{sat}} := 373 \text{ K}$$

$$\Delta T_e := T_s - T_{\text{sat}} \quad \Delta T_e = 17 \text{ K}$$

Since the surface temperature would cause an excess temperature that is in the nucleate boiling range for water at atmospheric pressure ( $5 < T_e < 30$ ), we have nucleate boiling occurring.

Using Rohsenow's correlation, 10.5 and constants from Table 10.1

$$C_{sf} := 0.0132 \quad n := 1.0$$

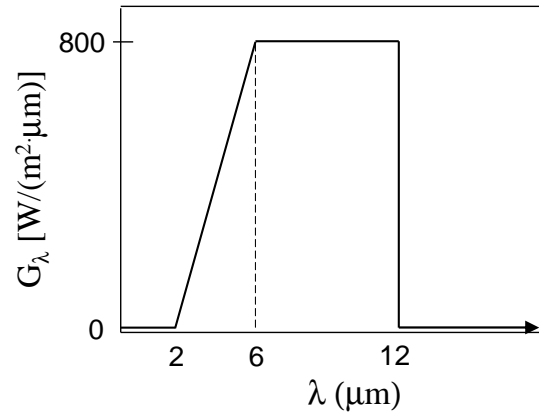
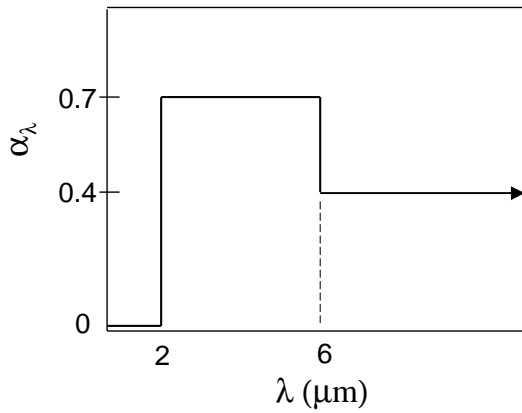
$$q_{\text{boiling}} := A \cdot \mu_l \cdot h_{fg} \cdot \left[ \frac{g \cdot (\rho_l - \rho_v)}{\sigma_{st}} \right]^{\frac{1}{2}} \cdot \left( \frac{c_{p,l} \Delta T_e}{C_{sf} \cdot h_{fg} \cdot Pr_l^n} \right)^3$$

$$q_{\text{boiling}} = 6.419 \times 10^3 \text{ W}$$

In this case, radiation can be neglected since  $q_{\text{rad}} \ll q_{\text{boiling}}$



3. (18 points) An opaque, diffuse surface has a spectral, hemispherical absorptivity and spectral irradiation as shown in the two figures below.



- (6 points) Using the spectral absorptivity ( $\alpha_\lambda$ ) and the given irradiation values over the spectral range ( $G_\lambda$ ), calculate the total, hemispherical absorptivity of the surface.
- (6 points) What is the total, hemispherical emissivity of the surface when the surface is at a temperature of 1000 K?
- (2 points) Is the surface gray? Explain.
- (4 points) If the surface is initially at 1000 K as above, show whether the surface temperature will increase or decrease after being exposed to the irradiation (neglecting conduction and convection).

Given

$$\begin{aligned}\alpha_{\lambda_1} &:= 0.7 & \lambda_1 &:= 2 & T_s &:= 1000\text{K} \\ \alpha_{\lambda_2} &:= 0.4 & \lambda_2 &:= 6 & \sigma &:= 5.67 \cdot 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4} \\ & & \lambda_3 &:= 12 & & \end{aligned}$$

a)

$$G_{2\_6} := \frac{800}{2} \frac{\text{W}}{\text{m}^2}$$

$$G_{6\_12} := 800 \frac{\text{W}}{\text{m}^2}$$

$$G_{\text{abs}} := \alpha_{\lambda_1} \cdot G_{2\_6} (\lambda_2 - \lambda_1) + \alpha_{\lambda_2} \cdot G_{6\_12} (\lambda_3 - \lambda_2) \quad G_{\text{abs}} = 3.04 \times 10^3 \frac{\text{W}}{\text{m}^2}$$

$$G := G_{2\_6} (\lambda_2 - \lambda_1) + G_{6\_12} (\lambda_3 - \lambda_2) \quad G = 6.4 \times 10^3 \frac{\text{W}}{\text{m}^2}$$

$$\alpha := \frac{G_{\text{abs}}}{G} \quad \alpha = 0.475$$

b)

Since the surface is diffuse:  $\epsilon_{\lambda} := \alpha_{\lambda}$

$$\lambda T_{1.\text{rad}} := \lambda_1 \cdot T_s \quad \lambda T_{1.\text{rad}} = 2 \times 10^3 \text{ K} \quad \rightarrow \quad F_{1.\text{rad}} := 0.066728$$

$$\lambda T_{2.\text{rad}} := \lambda_2 \cdot T_s \quad \lambda T_{2.\text{rad}} = 6 \times 10^3 \text{ K} \quad \rightarrow \quad F_{2.\text{rad}} := 0.737818$$

$$\epsilon := \alpha_{\lambda_1} (F_{2.\text{rad}} - F_{1.\text{rad}}) + \alpha_{\lambda_2} (1 - F_{2.\text{rad}}) \quad \epsilon = 0.575$$

c)

The surface is not gray since the total hemispherical emissivity does not equal the total hemispherical absorptivity.

d)

$$q_{\text{rad}} := \epsilon \cdot \sigma \cdot T_s^4 \quad q_{\text{rad}} = 3.258 \times 10^4 \frac{\text{W}}{\text{m}^2}$$

$$q_{\text{net}} := G_{\text{abs}} - q_{\text{rad}} \quad q_{\text{net}} = -2.954 \times 10^4 \frac{\text{W}}{\text{m}^2}$$

Therefore, the surface temperature will decrease since  $q_{\text{rad}} > G_{\text{abs}}$