

**EE321 Exam 1
Spring 2009**

Notes: Write your name and ID on blue book. This part of exam will be recycled.

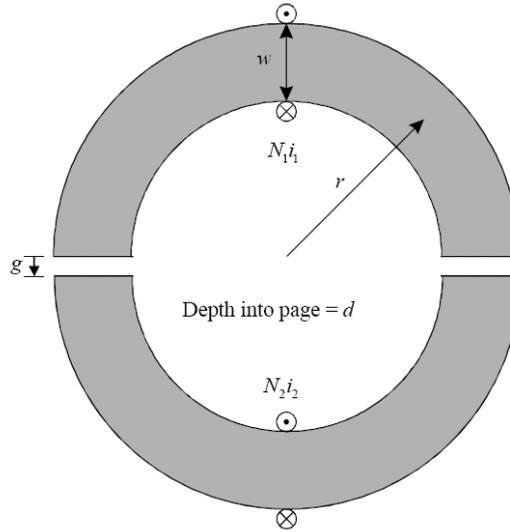
You must show work for credit, except for problem 6.

Achieving a score of 60% or above on this exam satisfies ABET Objective 1 and Objective 2.

Good luck !

- 1.) 10 pts. Consider a Cartesian coordinate system. Suppose there exists a uniform H-field with a +10 A/m component in the x-direction, a +20 A/m component in the y-direction, and a -5 A/m component in the z-direction. What is the magneto motive force drop between the starting point (5,2,1) (x, y, z) and the ending point (4,2,4).

For problems 2-3, consider the split toroid shown below. The cross section of the toroid is rectangular.



- 2.) 15 pts. The permeability of the magnetic material in the split toroid may be expressed

$$\mu_B(B) = \mu_0 \frac{5000}{1 + |B|}$$

where μ_0 is the permeability of free space, $4\pi 10^{-7}$ H/m. Now suppose $g = 1$ mm, $r = 10$ cm, $w = 1$ cm, $d = 2$ cm, $N_1 = 100$, $N_2 = 20$, and $i_1 = 5$ A. If the flux linking the second winding is $\lambda_2 = 0.004$ Vs, what is the current i_2 ? Hint $100 < i_2 < 200$.

- 3.) 20 pts. Assume that the relative permeability of the magnetic material in the toroid is constant and has a value μ_r . Derive an expression of the electromagnetic force on the lower half of the toroid. Your expression should be in terms of the following variables: w , d , r , N_1 , N_2 , i_1 , i_2 , g , μ_r , and μ_0 . The desired result is symbolic – do not use the numbers from problem 2!

- 4.) 15 pts. Consider a magnetic system with the following flux linkage equations

$$\begin{aligned}\lambda_1 &= 2i_1 + 10 \sin(4\theta_m)(1 - e^{-2i_1 - i_2}) \\ \lambda_2 &= 3i_2 + 5 \sin(4\theta_m)(1 - e^{-2i_1 - i_2})\end{aligned}$$

where $i_1 \geq 0$ and $i_2 \geq 0$. Derive an expression for co-energy.

[CONTINUED ON NEXT PAGE]

5.) 10 pts. Consider a variable reluctance stepper motor. The flux linkage equation may be expressed

$$\lambda_{as} = \frac{1}{1000}(5 + 4 \cos(4\theta_{rm}))i_{as}$$

The winding resistance of the stepper motor is 5 Ohms, and the supply voltage for the stepper motor circuit is 10 V. There are 5 phases. 5a) What is the step length ? { 5 pts}. Neglecting semiconductor voltage drops, what is the holding torque ? { 5 pts}.

The following questions should be answered true or false. They are worth 1 pt. each. You do not need to show work.

- 6a) Ferrimagnetic materials have higher saturation flux densities than ferromagnetic materials.
- 6b) In an inductor, most of the energy is stored in the magnetic material.
- 6c) Magnetic saturation causes a magnetic field not to be conservative.
- 6d) The atoms in ferromagnetic materials have magnetic moments that are aligned in an anti-parallel fashion.
- 6e) Some stepper motors use permanent magnets
- 6f) Coenergy and field energy are equal in linear magnetic systems.
- 6g) The following system is magnetically linear

$$\lambda = \frac{1}{2+x}i$$

- 6h) Ohm's law is easier to break than Kirchoff's voltage law.
- 6i) Any set of flux linkage equations one might write possess the properties of a conservative field
- 6j) Multistack variable reluctance stepper motors are never built with just two phases.