Industrial Engineering 546
Spring 2019
Economic Decisions in Engineering

## Exam 1

## Directions:

- You have 75 minutes to complete this exam. If you open the test before stated or do not turn it in on time you will automatically lose 20 points.
- You are allowed a single $8 \frac{1}{2} \times 11$ inch sheet, with notes front and back. Otherwise, this exam is closed book and notes.
- Your are allowed to use a calculator (graphing or simple). No other electronic devices are permitted.
- Your answers must be legible. Circle, underline, or leave sufficient white-space to distinguish your answers from intermediate work.
- Show all your work.
- Write your name and PUID on each sheet.
- Do not write along the edge of the paper or on the back-side. The final pages are blank and you may use them for scratch work or overflow.


## Grade:

1. [35] $\qquad$
2. [30] $\qquad$
3. [15] $\qquad$
4. [5] $\qquad$
5. [15] $\qquad$

Total: $\qquad$

Problem 1. [35 points] A farmer hears of potential bad weather next week. He can pay $\$ C$ to take protective action to save his crop. If he does not take protective action, with probability $p$ his crop will be severely damaged and he will incur a loss of $\$ L$. The following decision tree models his decision.


|  | low | base | high |
| :---: | :---: | :---: | :---: |
| $p$ | $10 \%$ | $20 \%$ | $50 \%$ |
| $C$ | 10 k | 20 k | 40 k |
| $L$ | 50 k | 100 k | 200 k |

Conduct sensitivity analysis. First determine the expected costs of each alternative using the base-case values:
$\mathrm{E}[$ cost of taking protective action $]=$

$$
\mathrm{E}[\text { cost of taking no action }]=
$$

|  | low | base | high |
| :---: | :---: | :---: | :---: |
| $p$ | $10 \%$ | $20 \%$ | $50 \%$ |
| $C$ | 10 k | 20 k | 40 k |
| $L$ | 50 k | 100 k | 200 k |

Draw the one-way sensitivity plots for $p$ and $L$. Label the curves.



What is the advantage of a one-way sensitivity plot compared to a tornado diagram?

|  | low | base | high |
| :---: | :---: | :---: | :---: |
| $p$ | $10 \%$ | $20 \%$ | $50 \%$ |
| $C$ | 10 k | 20 k | 40 k |
| $L$ | 50 k | 100 k | 200 k |

Draw the tornado diagrams for strategies 'no action' and 'protective action.' Label the axes.


What is the advantage of a tornado diagram to a one-way sensitivity plot?

|  | low | base | high |
| :---: | :---: | :---: | :---: |
| $p$ | $10 \%$ | $20 \%$ | $50 \%$ |
| $C$ | 10 k | 20 k | 40 k |
| $L$ | 50 k | 100 k | 200 k |

Draw the two-way sensitivity plot for $p$ and $C$. For each region, denote the preferred strategy. (Recall the values are costs, so smaller is better.)

Two-way sensitivity plot for pand C


What is the preferred alternative on the boundary itself?

Based on the results of the sensitivity analysis, what should the farmer do next in modeling this decision, if anything?

Problem 2. [30 points]
We'll stick with helping out our farmer friend. He is considering consulting a clairvoyant ${ }^{1}$.


|  | low | base | high |
| :---: | :---: | :---: | :---: |
| $p$ | $10 \%$ | $20 \%$ | $50 \%$ |
| $C$ | 10 k | 20 k | 40 k |
| $L$ | 50 k | 100 k | 200 k |

Suppose he has access to perfect information about whether there would be damage. Draw the augmented decision tree.

What is the Value of Perfect Information? Using base case values for variables $p, C$, and $L$. (Recall the expected values are costs, so smaller is better. You may also convert the costs to gains by writing "-C" and "-L" in the tree above.)

[^0]

|  | low | base | high |
| :---: | :---: | :---: | :---: |
| $p$ | $10 \%$ | $20 \%$ | $50 \%$ |
| $C$ | 10 k | 20 k | 40 k |
| $L$ | 50 k | 100 k | 200 k |

Now suppose he is considering consulting with two imperfect clairvoyants, $M$ and $J$.
Draw the augmented decision tree (without probabilities) for this decision. Do not calculate probabilities here.


|  | low | base | high |
| :---: | :---: | :---: | :---: |
| $p$ | $10 \%$ | $20 \%$ | $50 \%$ |
| $C$ | 10 k | 20 k | 40 k |
| $L$ | 50 k | 100 k | 200 k |

Consider the two imperfect clairvoyants, $M$ and $J$. Their statements are independent conditioned on the event. They have accuracies of $70 \%$ and $90 \%$ respectively. For example

$$
\begin{aligned}
P(M \text { says loss }, J \text { says no loss } \mid \text { loss }) & =P(M \text { says loss } \mid \text { loss }) P(J \text { says no loss } \mid \text { loss }) \\
& =(0.70)(1-0.90)
\end{aligned}
$$

What is $P(M$ says loss , $J$ says no loss $)$ ? (use $p=0.2$ )

What is $P($ no loss $\mid M$ says loss , $J$ says no loss $)$ ? (use $p=0.2)$

## Problem 3. [15 points]

A. Your friend Al wants to borrow $\$ 100 \mathrm{k}$ for his business. He promises to pay you $\$ 125 \mathrm{k}$ 5 years from now. What is the net present value of this deal? Assume $3 \%$ inflation.
B. Your friend Al wants to borrow $\$ 100 \mathrm{k}$ for his business. He promises to pay you back 5 years from now. How much should he pay you so you can make a profit of $\$ 25 \mathrm{k}$ (in 2019 dollars)? Assume 3\% inflation.
C. Instead of lending your $\$ 100 \mathrm{k}$ to Al , you consider investing it in an account with $6 \%$ annual interest. How many years will it take for the value (in 2019 dollars) to triple? Assume 3\% inflation.

Problem 4. [5 points] Draw a fundamental objective hierarchy for buying personal computer. The hierarchy should have at least two layers (below overall objective) and at least ten total objectives (in addition to the overall objective). Do not determine trade-off coefficients (e.g. calculate an overall score).

Problem 5. [15 points] Consider you are a manager at an oil firm deciding where to drill for oil. There are two sites you are considering drilling at, and payoffs are listed in the tree below.

Construct a regret table for this decision and determine what strategy is best according to minimax regret.


Explain in your own words what minimax regret is.


[^0]:    ${ }^{1}$ Since our farmer does not have money for consulting firms, he'd look to Miss Cleo, John Edward, or a fortune cookie from that Chinese restaurant down the street.

